

UNIVERSITY OF CAMBRIDGE INTERNATIONAL EXAMINATIONS International General Certificate of Secondary Education

	CANDIDATE NAME		
	CENTRE NUMBER		CANDIDATE NUMBER
* 8 5	MATHEMATICS		0580/04
5 7	Paper 4 (Extende	d)	October/November 2009
•			2 hours 30 minutes
	Candidates answe	er on the Question Paper.	
7 2 7 *	Additional Materia	als: Electronic calculator Mathematical tables (optional)	Geometrical instruments Tracing paper (optional)

READ THESE INSTRUCTIONS FIRST

Write your Centre number, candidate number and name on all the work you hand in.

Write in dark blue or black pen.

You may use a soft pencil for any diagrams or graphs.

Do not use staples, paper clips, highlighters, glue or correction fluid.

Answer all questions.

If working is needed for any question it must be shown below that question.

Electronic calculators should be used.

If the degree of accuracy is not specified in the question, and if the answer is not exact, give the answer to three significant figures. Give answers in degrees to one decimal place.

For π use either your calculator value or 3.142.

At the end of the examination, fasten all your work securely together.

The number of marks is given in brackets [] at the end of each question or part question. The total of the marks for this paper is 130.

For Examiner's Use

This document consists of 21 printed pages and 3 blank pages.



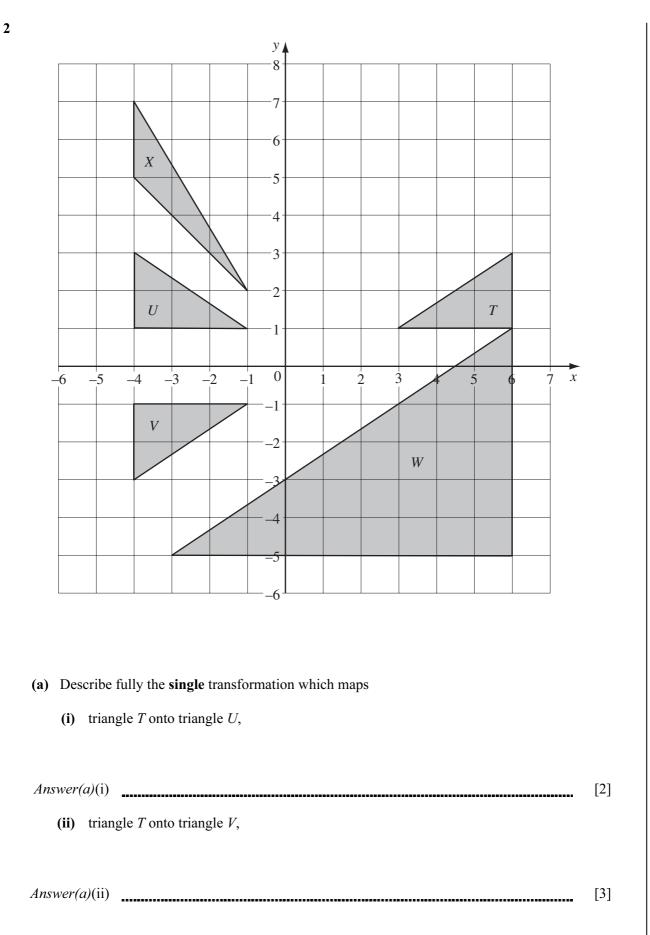
1	Chi	ris go	es to a shop to buy meat, vegetables and fruit.	For Examiner's
	(a)	(i)	The costs of the meat, vegetables and fruit are in the ratio	Use
			meat : vegetables : fruit = $2 : 2 : 3$.	
			The cost of the meat is \$2.40.	
			Calculate the total cost of the meat, vegetables and fruit.	
			Answer(a)(i) [2]	
		(ii)	Chris pays with a \$20 note.	
			What percentage of the \$20 has he spent?	
			Answer(a)(ii) % [2]	
	(b)	The	e masses of the meat, vegetables and fruit are in the ratio	
			meat : vegetables : fruit = $1 : 8 : 3$.	
		The	e total mass is 9 kg.	
		Cal	culate the mass of the vegetables.	
			(
			Answer(b) kg [2]	

(c) Calculate the cost per kilogram of the fruit.

Answer(c) \$ [3]

(d) The cost of the meat, \$2.40, is an increase of 25% on the cost the previous week.Calculate the cost of the meat the previous week.

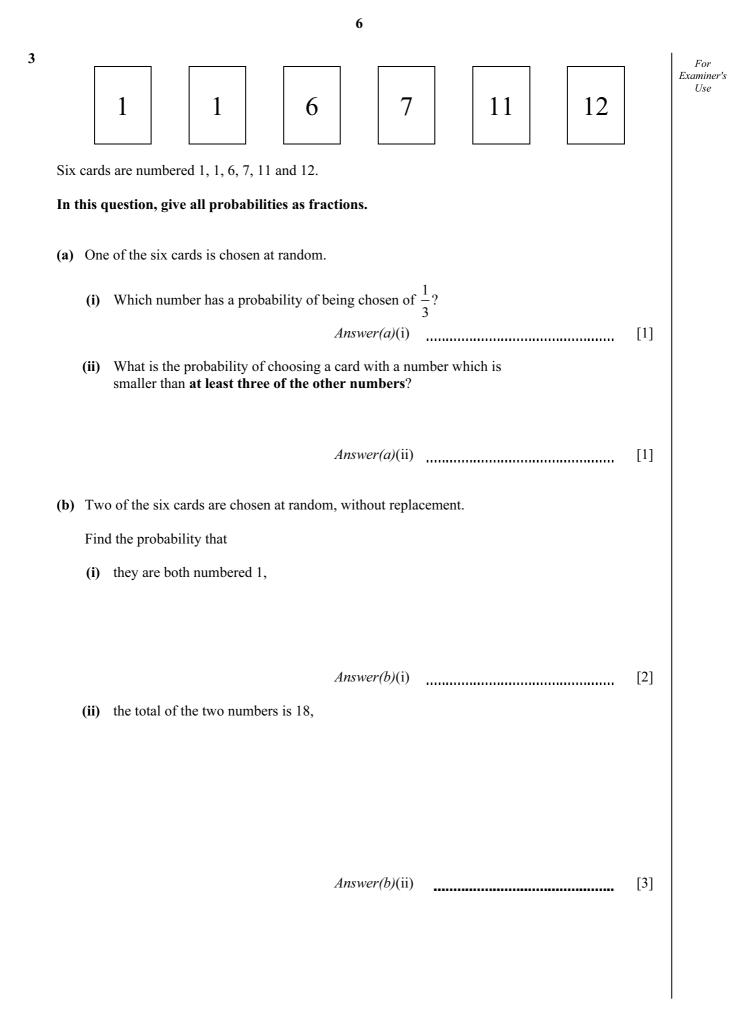
Answer(d) \$ [2]

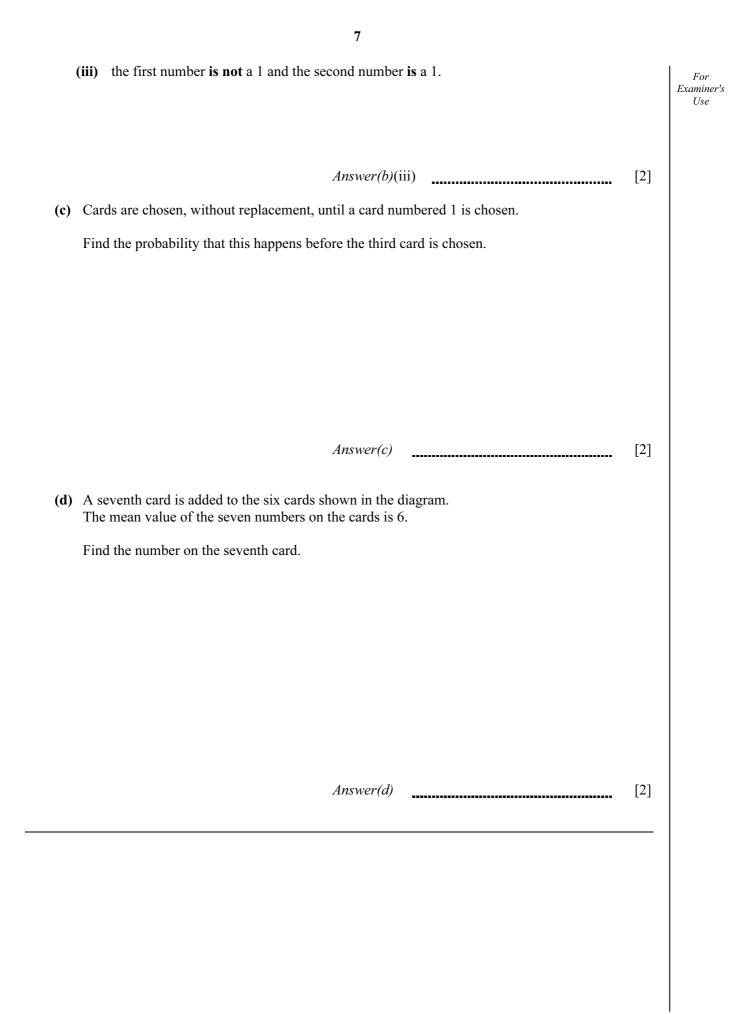


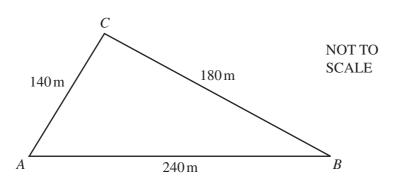
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5







The boundary of a park is in the shape of a triangle *ABC*. AB = 240 m, BC = 180 m and CA = 140 m.

In part (a), show clearly all your construction arcs.

(a) (i) Using a scale of 1 centimetre to represent 20 metres, **construct** an **accurate** scale drawing of triangle *ABC*. The line *AB* has already been drawn for you.

1	1	D					
		[2]				
(ii)	Using a straight edge and compasses only, construct the bisector of angle AC	Ъ.					
		_					
	Label the point D , where this bisector meets AB .	l	2]				
(iii)	Using a straight edge and compasses only, construct the locus of points, insid	la tha triang	10				
(111)	which are equidistant from A and from D.	•	[2]				
	when are equidistant from 7 and from D.	l					
(iv)	Flowers are planted in the park so that they are nearer to AC than to BC and nearer						
	to D than to A.						
	Shade the region inside your triangle which shows where the flowers are plan	ted. [[1]				

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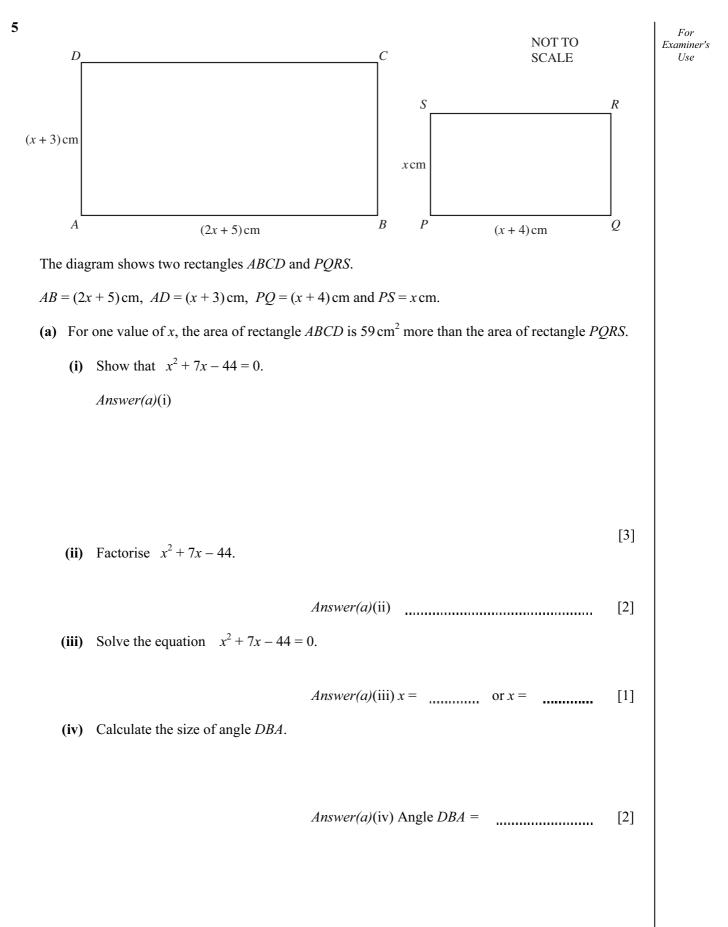
Λ

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B

par	rt (a).		
(b)	(i)	Show clearly that angle ACB is 96.4°.	
		Answer(b)(i)	
			[3]
	(ii)	Calculate the area of the park.	
		Answer(b)(ii) m ²	[2]
	(iii)	Use the sine rule to calculate angle <i>ABC</i> .	
		Answer(b)(iii) Angle ABC =	[3]

In part (b), use trigonometry. You must show your working and must NOT use any measurements from your construction in part (a).



- (b) For a different value of *x*, the rectangles *ABCD* and *PQRS* are similar.
 - (i) Show that this value of x satisfies the equation $x^2 2x 12 = 0$. Answer(b)(i)

[3]

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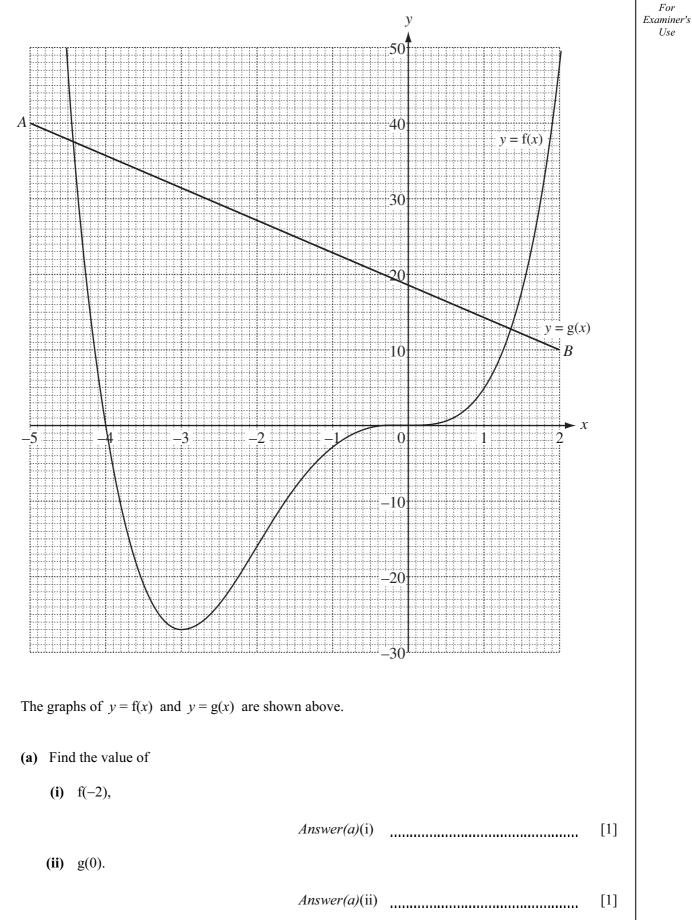
(ii) Solve the equation $x^2 - 2x - 12 = 0$, giving your answers correct to 2 decimal places.

Answer(b)(ii) x = _____ or x = _____ [4]

(iii) Calculate the perimeter of the rectangle PQRS.

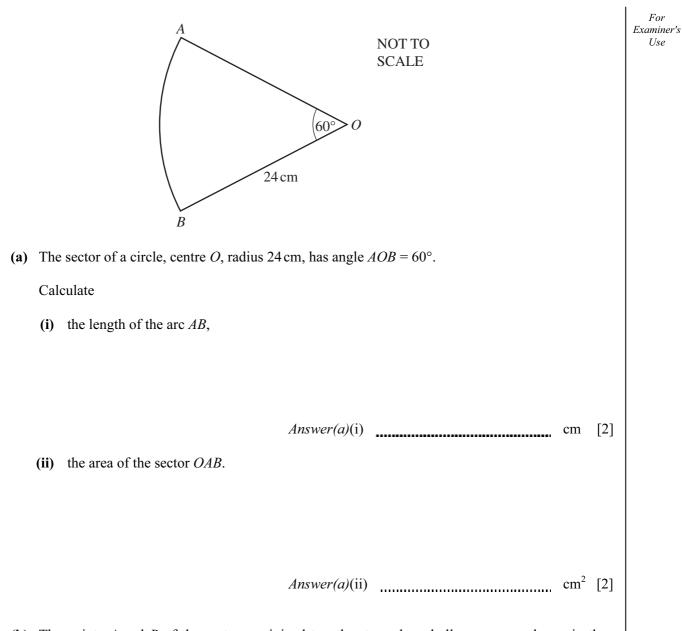
Answer(b)(iii) cm [1]



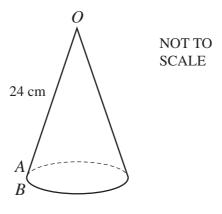


(b) Use the graphs to solve For Examiner's Use(i) the equation f(x) = 20, $Answer(b)(i) x = \qquad \text{or } x =$ [2] (ii) the equation f(x) = g(x), Answer(b)(ii) x = or x =[2] (iii) the inequality f(x) < g(x). Answer(b)(iii) [1] (c) Use the points A and B to find the gradient of y = g(x) as an exact fraction. Answer(c) [2] (d) On the grid, draw the graph of y = g(x) - 10. [2] (e) (i) Draw the tangent to the graph of y = f(x) at (-3, -27). [1] (ii) Write down the equation of this tangent. Answer(e)(ii) [1] (f) A region, R, contains points whose co-ordinates satisfy the inequalities $-3 \leq x \leq -2$, $y \leq 40$ and $y \ge g(x)$. On the grid, draw suitable lines and label this region R. [2]

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(b) The points A and B of the sector are joined together to make a hollow cone as shown in the diagram. The arc AB of the sector becomes the circumference of the base of the cone.



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8 Fifty students are timed when running one kilometre.

The results are shown in the table.

Time (<i>t</i> minutes)	$4.0 < t \le 4.5$	$4.5 < t \le 5.0$	$5.0 < t \le 5.5$	$5.5 < t \le 6.0$	$6.0 < t \le 6.5$	$6.5 < t \le 7.0$	
Frequency	2	7	8	18	10	5	

(a) Write down the modal time interval.

Answer(a) min [1]

(b) Calculate an estimate of the mean time.

Answer(b) min [4]

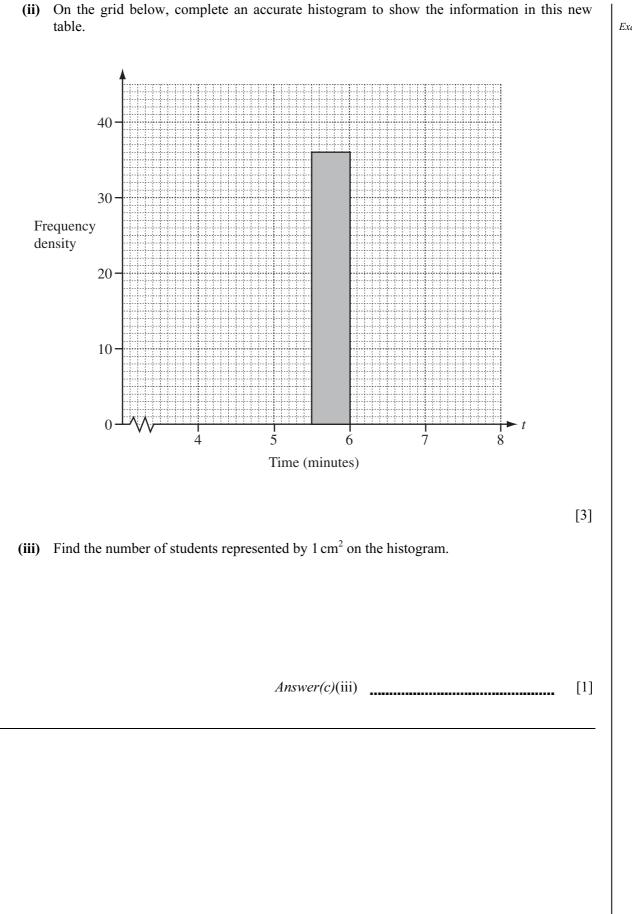
(c) A new frequency table is made from the results shown in the table above.

Time (<i>t</i> minutes)	$4.0 < t \le 5.5$	$5.5 < t \le 6.0$	$6.0 < t \le 7.0$
Frequency		18	

(i) Complete the table by filling in the two empty boxes.

[1]

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(iii) Solve the equation
$$\frac{3}{x-1} - \frac{2}{x+3} = \frac{1}{x}$$
.

Answer(b)(iii) x =[3] -----

(c)
$$p = \frac{t}{q-1}$$

Find q in terms of p and t.

Answer(c) q =



									Total	
Row 1							1	=	1	
Row 2					3	+	5	=	8	
Row 3			7	+	9	+	11	=	27	
Row 4	13	+	15	+	17	+	19	=	64	
Row 5										
Row 6										
The rows above show sets of consecutive o	dd nun	ıber	s and	l the	ir tot	als.				
(a) Complete Row 5 and Row 6.										[2]
(b) What is the special name given to the n	number	s 1,	8, 27	7,64	ł?					
	A	1 <i>ns</i> v	ver(b)						[1]
(c) Write down in terms of <i>n</i> ,										
(i) how many consecutive odd numb	ers the	re ai	e in	Row	/ n .					
()										[1]
(ii) the total of these numbers	E		/er(c	(1)	•••••					[1]
(ii) the total of these numbers.										
)(ii)						[1]
(d) The first number in Row <i>n</i> is given by	$n^2 - r$	i + 1								
Show that this formula is true for Row	4.									
Answer(d)										

[1]

(e) The total of Row 3 is 27. This can be calculated by $(3 \times 7) + 2 + 4$. Examiner's The total of Row 4 is 64. This can be calculated by $(4 \times 13) + 2 + 4 + 6$. The total of Row 7 is 343. Show how this can be calculated in the same way. Answer(e) [1] (f) The total of the first *n* even numbers is n(n + 1). Write down a formula for the total of the first (n-1) even numbers. Answer(f) [1] (g) Use the results of parts (d), (e) and (f) to show clearly that the total of the numbers in Row n gives your answer to part (c)(ii).

Answer(g)

[2]

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